

Solving Equations & Inequalities

Class Goals – *By the end of the period, you will understand and be able to...*

- Solve Equations.
- Solve Inequalities.
- Solve Absolute Value Equations & Inequalities.

Pre-Requisite Exercises

One-Step Equations

1. $x + 6 = 10$

$$\begin{array}{r} -6 \quad -6 \\ \hline x = 4 \quad \checkmark \end{array}$$

2. $x - 1 = -5$

$$\begin{array}{r} +1 \quad +1 \\ \hline x = -4 \quad \checkmark \end{array}$$

3. $2x = 11$

$$\begin{array}{r} 2 \quad 2 \\ \hline x = 5.5 \quad \checkmark \end{array}$$

4. $3x \cdot \frac{x}{3} = 6x \cdot 3$

$$x = 18 \quad \checkmark$$

Two-Step Equations

5. $5x - 3 = -18$

$$\begin{array}{r} +3 \quad +3 \\ \hline 5x = -15 \\ \hline \frac{5x}{5} = \frac{-15}{5} \\ x = -3 \quad \checkmark \end{array}$$

6. $\frac{x}{3} - 2 = 6$

$$\begin{array}{r} +2 \quad +2 \\ \hline \frac{x}{3} = 8 \\ \hline \frac{x}{3} \cdot 3 = 8 \cdot 3 \\ x = 24 \quad \checkmark \end{array}$$

Multiplied by the reciprocal

7. $\frac{1}{4}x = 8$

$$\begin{array}{r} \frac{1}{4}x = 8 \\ \hline \frac{1}{4}x \cdot 4 = 8 \cdot 4 \\ x = 32 \quad \checkmark \end{array}$$

Multi-Step Equations

8. $3(x + 5) = 15$

$$\begin{array}{r} 3x + 15 = 15 \\ -15 \quad -15 \\ \hline 3x = 0 \\ \hline \frac{3x}{3} = \frac{0}{3} \\ x = 0 \quad \checkmark \end{array}$$

9. $\frac{2}{3}x - 1 = x + 7$

$$\begin{array}{r} 2x - 3 = 3x + 21 \\ -2x \quad -2x \\ \hline -3 = x + 21 \\ -21 \quad -21 \\ \hline -24 = x \quad \checkmark \end{array}$$

10. $\frac{1}{2}x + \frac{2}{3} = \frac{10}{7}$

Evaluating Absolute Value Expressions

11. $|12 + 7|$

12. $|5 - 9|$

13. $3|5 - 1|$

14. $5 - |2 - 7|$

15. $\frac{1}{2}|10 - 16| + 24$

16. $\frac{|12 - 18|}{3} + 7|2 - 5|$

Solving Equations

a. $2x + 6 = 3x - 5$

b. $3(5 - x) = 6 - 3x$

c. $\frac{1}{2}x + \frac{2}{3} = \frac{8}{5}$

Practice Problems – Solve the equations and check your solutions.

1. $4 - x = 2$

2. $4x = 2x - 12$

3. $\frac{x}{4} + 6 = -8$

4. $x + 4 = 2x - 5$

5. $-(x + 1) = 2(3x - 1)$

6. $\frac{3}{2}(x - 5) = 7$

Solving Absolute Value Equations

$$|2x + 5| = 21$$

Step 1:

Step 2:

Step 3:

Practice Problems – Solve the absolute value equations and check your solutions.

7. $|4x - 2| = 6$

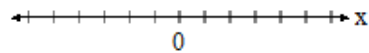
8. $|5 - x| = 6$

9. $|-2x + 1| - 3 = 11$

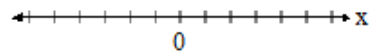
10. $|2x + 7| = 13$

Graphing Inequalities

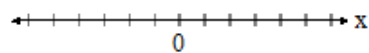
a. $x > 2$



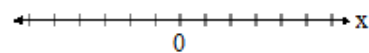
b. $x \leq -1$



c. $x \geq -4$



d. $x < 3$



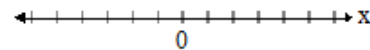
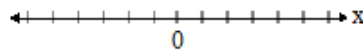
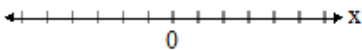
Open Circle vs. Closed Circle

Solving & Graphing Inequalities

a. $3x + 6 \geq 9$

b. $-2x - 3 > -5$

c. $3 < 4x - 5 < 27$

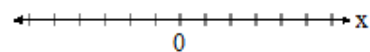
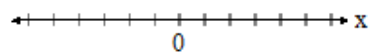


What must you remember when solving inequalities?

Practice Problems – Solve the inequality and graph on a number line.

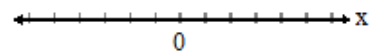
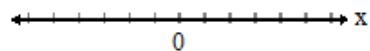
11. $2(x - 3) > -4$

12. $3 - 2x \geq 7$



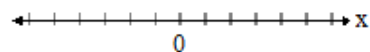
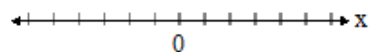
13. $2x + 4 < x + 3$

14. $2(x + 3) < 8$



15. $3 < \frac{1}{2}x - 1 < 5$

16. $3 - x \geq 2$



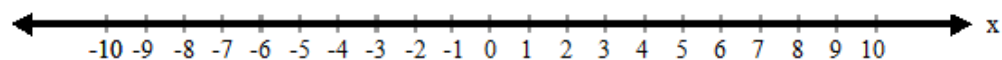
Solving Absolute Value Inequalities

$$|2x+1| > 5$$

Step 1:

Step 2:

Step 3:



Practice Problems – Solve the absolute value inequality and graph your solution.

17. $\left| \frac{x}{2} + 3 \right| < 2$

18. $|2 - 4x| \geq 10$

